

## The Python Programming Language: Functions

In [1]:

```
x = 1
y = 2
x + y
```

Out[1]:

3

In [2]:

```
x
```

Out[2]:

1

`add_numbers` is a function that takes two numbers and adds them together.

In [4]:

```
def add_numbers(x, y):
    return x + y

add_numbers(111, 232)
```

Out[4]:

343

`add_numbers` updated to take an optional 3rd parameter. Using `print` allows printing of multiple expressions within a single cell.

In [6]:

```
def add_numbers(x, y, z=None):
    if (z==None):
        return x+y
    else:
        return x+y+z

print(add_numbers(1, 2))
print(add_numbers(1, 2, 3)) # ceci est un commentaire
```

3

6

`add_numbers` updated to take an optional flag parameter.

In [5]:

```
def add_numbers(x, y, z=None, flag=False):
    if (flag):
```

```
    print('Flag is true!')
    if (z==None):
        return x + y
    else:
        return x + y + z

print(add_numbers(1, 2, flag=True))
```

```
Flag is true!
3
```

Assign function `add_numbers` to variable `a`.

In [6]:

```
def add_numbers(x,y):
    return x+y

a = add_numbers
a(1,2)
```

Out[6]:

```
3
```

## The Python Programming Language: Types and Sequences

Use `type` to return the object's type.

In [7]:

```
type('This is a string')
```

Out[7]:

```
str
```

In [8]:

```
type(None)
```

Out[8]:

```
NoneType
```

In [9]:

```
type(1)
```

Out[9]:

```
int
```

In [10]:

```
type(1.0)
```

Out[10]:

```
float
```

In [11]:

```
type(add_numbers)
```

```
Out[11]:
```

```
function
```

**Tuples are an immutable data structure (cannot be altered).**

```
In [12]:
```

```
x = (1, 'a', 2, 'b')
type(x)
```

```
Out[12]:
```

```
tuple
```

**Lists are a mutable data structure.**

```
In [7]:
```

```
x = [1, 'a', 2, 'b']
type(x)
```

```
Out[7]:
```

```
list
```

**Use `append` to append an object to a list.**

```
In [8]:
```

```
x.append(3.3)
print(x)
```

```
[1, 'a', 2, 'b', 3.3]
```

**This is an example of how to loop through each item in the list.**

```
In [10]:
```

```
for item in x:
    print(item)

print(len(x))
```

```
1
a
2
b
3.3
5
```

**Or using the indexing operator:**

```
In [14]:
```

```
i=0
while( i != len(x) ):
    print(x[i])
    i = i + 1

print('on est en dehors de la boucle while')
```

```
1
```

a  
2  
b  
3.3

on est en dehors de la boucle while

**Use `+` to concatenate lists.**

In [17]:

```
[1,2] + [3,4]
```

Out[17]:

```
[1, 2, 3, 4]
```

**Use `*` to repeat lists.**

In [15]:

```
[1, 2]*3
```

Out[15]:

```
[1, 2, 1, 2, 1, 2]
```

**Use the `in` operator to check if something is inside a list.**

In [23]:

```
4 in [1, 2, 3]
```

Out[23]:

```
False
```

**Now let's look at strings. Use bracket notation to slice a string.**

In [24]:

```
x = 'This is a string'  
print(x[0]) #first character  
print(x[0:1]) #first character, but we have explicitly set the end character  
print(x[0:2]) #first two characters
```

```
T  
T  
Th
```

**This will return the last element of the string.**

In [25]:

```
x[-1]
```

Out[25]:

```
'g'
```

**This will return the slice starting from the 4th element from the end and stopping before the 2nd element from the end.**

In [26]:

```
x[-4:-2]
```

Out[26]:

```
'ri'
```

**This is a slice from the beginning of the string and stopping before the 3rd element.**

In [27]:

```
x[:3]
```

Out[27]:

```
'Thi'
```

**And this is a slice starting from the 3rd element of the string and going all the way to the end.**

In [28]:

```
x[3:]
```

Out[28]:

```
's is a string'
```

In [29]:

```
firstname = 'Christopher'
lastname = 'Brooks'

print(firstname + ' ' + lastname)
print(firstname*3)
print('Chris' in firstname)
```

```
Christopher Brooks
ChristopherChristopherChristopher
True
```

`split` returns a list of all the words in a string, or a list split on a specific character.

In [30]:

```
firstname = 'Christopher Arthur Hansen Brooks'.split(' ')[0] # [0] selects the first element of the list
lastname = 'Christopher,Arthur,Hansen,Brooks'.split(',')[1] # [-1] selects the last element of the list
print(firstname)
print(lastname)
```

```
Christopher
Brooks
```

**Make sure you convert objects to strings before concatenating.**

In [27]:

```
'Chris' + 2
```

```
-----
TypeError                                 Traceback (most recent call last)
<ipython-input-27-9d01956b24db> in <module>()
----> 1 'Chris' + 2
```

**TypeError:** must be str, not int

In [28]:

```
'Chris' + str(2)
```

Out[28]:

```
'Chris2'
```

### Dictionaries associate keys with values.

In [44]:

```
x = {'Christopher Brooks': 'broosch@umich.edu', 'Bill Gates': 'billg@microsoft.com'}  
x['Christopher Brooks'] # Retrieve a value by using the indexing operator
```

Out[44]:

```
'broosch@umich.edu'
```

In [45]:

```
x['Kevyn Collins-Thompson'] = None  
x['Kevyn Collins-Thompson']
```

In [42]:

```
x= {"Age": 18, "taille": 1.7}  
x["taille"]
```

Out[42]:

```
1.7
```

### Iterate over all of the keys:

In [43]:

```
for name in x:  
    print(name + ": " + str(x[name]))
```

```
Age: 18  
taille: 1.7
```

### Iterate over all of the values:

In [46]:

```
for email in x.values():  
    print(email)
```

```
broosch@umich.edu  
billg@microsoft.com  
None
```

### Iterate over all of the items in the list:

In [47]:

```
for name, email in x.items():  
    print(name)  
    print(email)
```

Christopher Brooks  
broosch@umich.edu  
Bill Gates  
billg@microsoft.com  
Kevyn Collins-Thompson  
None

**You can unpack a sequence into different variables:**

In [48]:

```
x = ('Christopher', 'Brooks', 'broosch@umich.edu')  
fname, lname, email = x
```

In [49]:

```
fname
```

Out[49]:

```
'Christopher'
```

In [50]:

```
lname
```

Out[50]:

```
'Brooks'
```

**Make sure the number of values you are unpacking matches the number of variables being assigned.**

In [51]:

```
x = ('Christopher', 'Brooks', 'broosch@umich.edu', 'Ann Arbor')  
fname, lname, email = x
```

```
-----  
ValueError                                Traceback (most recent call last)  
<ipython-input-51-d2c50ec4987a> in <module>()  
      1 x = ('Christopher', 'Brooks', 'broosch@umich.edu', 'Ann Arbor')  
----> 2 fname, lname, email = x
```

**ValueError:** too many values to unpack (expected 3)

## The Python Programming Language: More on Strings

In [52]:

```
print('Chris' + 2)
```

```
-----  
TypeError                                Traceback (most recent call last)  
<ipython-input-52-928a1e955b60> in <module>()  
----> 1 print('Chris' + 2)
```

**TypeError:** must be str, not int

In [53]:

```
print('Chris' + str(2))
```

```
Chris2
```

Python has a built in method for convenient string formatting.

In [40]:

```
sales_record = {
    'price': 3.24,
    'num_items': 4,
    'person': 'Chris'}

sales_statement = '{} bought {} item(s) at a price of {} each for a total of {}'

print(sales_statement.format(sales_record['person'],
                             sales_record['num_items'],
                             sales_record['price'],
                             sales_record['num_items']*sales_record['price']))
```

Chris bought 4 item(s) at a price of 3.24 each for a total of 12.96

## Reading and Writing CSV files

Let's import our datafile mpg.csv, which contains fuel economy data for 234 cars.

- **mpg** : miles per gallon
- **class** : car classification
- **cty** : city mpg
- **cyl** : # of cylinders
- **displ** : engine displacement in liters
- **drv** : f = front-wheel drive, r = rear wheel drive, 4 = 4wd
- **fl** : fuel (e = ethanol E85, d = diesel, r = regular, p = premium, c = CNG)
- **hwy** : highway mpg
- **manufacturer** : automobile manufacturer
- **model** : model of car
- **trans** : type of transmission
- **year** : model year

In [54]:

```
import csv

%precision 2

with open('mpg.csv') as csvfile:
    mpg = list(csv.DictReader(csvfile))

mpg[:3] # The first three dictionaries in our list.
```

Out[54]:

```
[OrderedDict([('', '1'),
              ('manufacturer', 'audi'),
              ('model', 'a4'),
              ('displ', '1.8'),
              ('year', '1999'),
              ('cyl', '4'),
              ('trans', 'auto(l5)'),
              ('drv', 'f'),
              ('cty', '18'),
              ('hwy', '29'),
              ('fl', 'p'),
              ('class', 'compact')]),
 OrderedDict([('', '2'),
              ('manufacturer', 'audi'),
              ('model', 'a4'),
```



```
OrderedDict([('displ', '1.8'),
            ('year', '1999'),
            ('cyl', '4'),
            ('trans', 'manual(m5)'),
            ('drv', 'f'),
            ('cty', '21'),
            ('hwy', '29'),
            ('fl', 'p'),
            ('class', 'compact']]),
OrderedDict([('', '3'),
            ('manufacturer', 'audi'),
            ('model', 'a4'),
            ('displ', '2'),
            ('year', '2008'),
            ('cyl', '4'),
            ('trans', 'manual(m6)'),
            ('drv', 'f'),
            ('cty', '20'),
            ('hwy', '31'),
            ('fl', 'p'),
            ('class', 'compact']])]
```

`csv.Dictreader` has read in each row of our csv file as a dictionary. `len` shows that our list is comprised of **234 dictionaries**.

In [55]:

```
len(mpg)
```

Out[55]:

234

`keys` gives us the column names of our csv.

In [56]:

```
mpg[0].keys()
```

Out[56]:

```
odict_keys(['', 'manufacturer', 'model', 'displ', 'year', 'cyl', 'trans', 'drv', 'cty', 'hwy', 'fl', 'class'])
```

**This is how to find the average cty fuel economy across all cars. All values in the dictionaries are strings, so we need to convert to float.**

In [57]:

```
sum(float(d['cty']) for d in mpg) / len(mpg)
```

Out[57]:

16.86

**Similarly this is how to find the average hwy fuel economy across all cars.**

In [58]:

```
sum(float(d['hwy']) for d in mpg) / len(mpg)
```

Out[58]:

23.44

Use `set` to return the unique values for the number of cylinders the cars in our dataset have.

In [59]:

```
cylinders = set(d['cyl'] for d in mpg)
cylinders
```

Out[59]:

```
{'4', '5', '6', '8'}
```

Here's a more complex example where we are grouping the cars by number of cylinder, and finding the average city mpg for each group.

In [47]:

```
CtyMpgByCyl = []

for c in cylinders: # iterate over all the cylinder levels
    summpg = 0
    cyltypecount = 0
    for d in mpg: # iterate over all dictionaries
        if d['cyl'] == c: # if the cylinder level type matches,
            summpg += float(d['cty']) # add the city mpg
            cyltypecount += 1 # increment the count
    CtyMpgByCyl.append((c, summpg / cyltypecount)) # append the tuple ('cylinder', 'avg
mpg')

CtyMpgByCyl.sort(key=lambda x: x[0])
CtyMpgByCyl
```

Out[47]:

```
[('4', 21.01), ('5', 20.50), ('6', 16.22), ('8', 12.57)]
```

Use `set` to return the unique values for the class types in our dataset.

In [48]:

```
vehicleclass = set(d['class'] for d in mpg) # what are the class types
vehicleclass
```

Out[48]:

```
{'2seater', 'compact', 'midsize', 'minivan', 'pickup', 'subcompact', 'suv'}
```

And here's an example of how to find the average highway mpg for each class of vehicle in our dataset.

In [49]:

```
HwyMpgByClass = []

for t in vehicleclass: # iterate over all the vehicle classes
    summpg = 0
    vclasscount = 0
    for d in mpg: # iterate over all dictionaries
        if d['class'] == t: # if the cylinder amount type matches,
            summpg += float(d['hwy']) # add the hwy mpg
            vclasscount += 1 # increment the count
    HwyMpgByClass.append((t, summpg / vclasscount)) # append the tuple ('class', 'avg mp
g')

HwyMpgByClass.sort(key=lambda x: x[1])
HwyMpgByClass
```

Out[49]:

Out [49]:

```
[('pickup', 16.88),  
 ('suv', 18.13),  
 ('minivan', 22.36),  
 ('2seater', 24.80),  
 ('midsize', 27.29),  
 ('subcompact', 28.14),  
 ('compact', 28.30)]
```

## The Python Programming Language: Dates and Times

In [50]:

```
import datetime as dt  
import time as tm
```

`time` returns the current time in seconds since the Epoch. (January 1st, 1970)

In [51]:

```
tm.time()
```

Out [51]:

```
1572685325.20
```

**Convert the timestamp to datetime.**

In [52]:

```
dtnow = dt.datetime.fromtimestamp(tm.time())  
dtnow
```

Out [52]:

```
datetime.datetime(2019, 11, 2, 10, 2, 7, 491539)
```

**Handy datetime attributes:**

In [53]:

```
dtnow.year, dtnow.month, dtnow.day, dtnow.hour, dtnow.minute, dtnow.second # get year, m  
onth, day, etc. from a datetime
```

Out [53]:

```
(2019, 11, 2, 10, 2, 7)
```

`timedelta` is a duration expressing the difference between two dates.

In [54]:

```
delta = dt.datetime.timedelta(days = 100) # create a timedelta of 100 days  
delta
```

Out [54]:

```
datetime.timedelta(100)
```

`datetime.datetime.now()` returns the current local date

`date.today` returns the current local date.

In [55]:

```
today = dt.date.today()
```

In [56]:

```
today - delta # the date 100 days ago
```

Out[56]:

```
datetime.date(2019, 7, 25)
```

In [57]:

```
today > today-delta # compare dates
```

Out[57]:

```
True
```

## The Python Programming Language: Objects and map()

An example of a class in python:

In [50]:

```
class Person:
    department = 'School of Information' #a class variable

    def set_name(self, new_name): #a method
        self.name = new_name
    def set_location(self, new_location):
        self.location = new_location
```

In [51]:

```
person = Person()
person.set_name('Christopher Brooks')
person.set_location('Ann Arbor, MI, USA')
print('{} live in {} and works in the department {}'.format(person.name, person.location
, person.department))
```

Christopher Brooks live in Ann Arbor, MI, USA and works in the department School of Information

Here's an example of mapping the `min` function between two lists.

In [52]:

```
store1 = [10.00, 11.00, 12.34, 2.34]
store2 = [9.00, 11.10, 12.34, 2.01]
cheapest = map(min, store1, store2)
cheapest
```

Out[52]:

```
<map at 0x12998ab05f8>
```

Now let's iterate through the map object to see the values.

In [53]:

```
for item in cheapest:  
    print(item)
```

```
9.0  
11.0  
12.34  
2.01
```

## The Python Programming Language: Lambda and List Comprehensions

Here's an example of lambda that takes in three parameters and adds the first two.

In [54]:

```
my_function = lambda a, b, c : a + b
```

In [55]:

```
my_function(1, 2, 3)
```

Out[55]:

```
3
```

Let's iterate from 0 to 999 and return the even numbers.

In [56]:

```
my_list = []  
for number in range(0, 1000):  
    if number % 2 == 0:  
        my_list.append(number)  
my_list
```

Out[56]:

```
[0,  
2,  
4,  
6,  
8,  
10,  
12,  
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988,  
990,  
992,  
994,  
996,  
998]
```

**Now the same thing but with list comprehension.**

In [65]:

```
my_list = [number for number in range(0,1000) if number % 2 == 0]  
my_list
```

Out[65]:

```
[0,  
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990,  
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996,  
998]
```

## The Python Programming Language: Numerical Python (NumPy)

In [60]:

```
import numpy as np
```

### Creating Arrays

Create a list and convert it to a numpy array

In [61]:

```
mylist = [1, 2, 3]
x = np.array(mylist)
x
```

Out[61]:

```
array([1, 2, 3])
```

### Or just pass in a list directly

In [62]:

```
y = np.array([4, 5, 6])
y
```

Out[62]:

```
array([4, 5, 6])
```

### Pass in a list of lists to create a multidimensional array.

In [63]:

```
m = np.array([[7, 8, 9], [10, 11, 12]])
m
```

Out[63]:

```
array([[ 7,  8,  9],
       [10, 11, 12]])
```

### Use the shape method to find the dimensions of the array. (rows, columns)

In [64]:

```
m.shape
```

Out[64]:

```
(2, 3)
```

`arange` returns evenly spaced values within a given interval.

In [67]:

```
n = np.arange(0, 100, 5) # start at 0 count up by 2, stop before 30
n.shape
```

Out[67]:

```
(20,)
```

`reshape` returns an array with the same data with a new shape.

In [68]:

```
n = n.reshape(4, 5) # reshape array to be 3x5
n
```

Out[68]:

```
array([[ 0,  5, 10, 15, 20],
       [25, 30, 35, 40, 45],
       [50, 55, 60, 65, 70],
       [75, 80, 85, 90, 95]])
```

[15, 20, 25, 30, 35]]

`linspace` returns evenly spaced numbers over a specified interval.

In [70]:

```
o = np.linspace(0, 4, 9) # return 9 evenly spaced values from 0 to 4
o
```

Out[70]:

```
array([0. , 0.5, 1. , 1.5, 2. , 2.5, 3. , 3.5, 4. ])
```

`resize` changes the shape and size of array in-place.

In [74]:

```
o.resize(3, 3)
o
```

Out[74]:

```
array([[0. , 0.5, 1. ],
       [1.5, 2. , 2.5],
       [3. , 3.5, 4. ]])
```

`ones` returns a new array of given shape and type, filled with ones.

In [71]:

```
np.ones((3, 2))
```

Out[71]:

```
array([[1., 1.],
       [1., 1.],
       [1., 1.]])
```

`zeros` returns a new array of given shape and type, filled with zeros.

In [72]:

```
np.zeros((2, 3))
```

Out[72]:

```
array([[0., 0., 0.],
       [0., 0., 0.]])
```

`eye` returns a 2-D array with ones on the diagonal and zeros elsewhere.

In [73]:

```
np.eye(3)
```

Out[73]:

```
array([[1., 0., 0.],
       [0., 1., 0.],
       [0., 0., 1.]])
```

`diag` extracts a diagonal or constructs a diagonal array.

In [74]:

```
np.diag(y)
```

Out[74]:

```
array([[4, 0, 0],
       [0, 5, 0],
       [0, 0, 6]])
```

**Create an array using repeating list (or see `np.tile`)**

In [75]:

```
np.array([1, 2, 3] * 3)
```

Out[75]:

```
array([1, 2, 3, 1, 2, 3, 1, 2, 3])
```

**Repeat elements of an array using `repeat`.**

In [76]:

```
np.repeat([1, 2, 3], 3)
```

Out[76]:

```
array([1, 1, 1, 2, 2, 2, 3, 3, 3])
```

## Combining Arrays

In [77]:

```
p = np.ones([2, 3], int)
p
```

Out[77]:

```
array([[1, 1, 1],
       [1, 1, 1]])
```

**Use `vstack` to stack arrays in sequence vertically (row wise).**

In [82]:

```
np.vstack([p, 2*p])
```

Out[82]:

```
array([[1, 1, 1],
       [1, 1, 1],
       [2, 2, 2],
       [2, 2, 2]])
```

**Use `hstack` to stack arrays in sequence horizontally (column wise).**

In [83]:

```
np.hstack([p, 2*p])
```

Out[83]:

```
array([[1, 1, 1, 2, 2, 2],
       [1, 1, 1, 2, 2, 2]])
```

## Operations

Use `+`, `-`, `*`, `/` and `**` to perform element wise addition, subtraction, multiplication, division and power.

In [78]:

```
print(x + y) # elementwise addition    [1 2 3] + [4 5 6] = [5 7 9]
print(x - y) # elementwise subtraction [1 2 3] - [4 5 6] = [-3 -3 -3]
```

```
[5 7 9]
[-3 -3 -3]
```

In [79]:

```
print(x * y) # elementwise multiplication [1 2 3] * [4 5 6] = [4 10 18]
print(x / y) # elementwise division      [1 2 3] / [4 5 6] = [0.25 0.4 0.5]
```

```
[ 4 10 18]
[0.25 0.4 0.5 ]
```

In [80]:

```
print(x**2) # elementwise power [1 2 3] ^2 = [1 4 9]
```

```
[1 4 9]
```

### Dot Product:

$$\begin{bmatrix} x_1 & x_2 & x_3 \end{bmatrix}$$
$$\cdot \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$
$$= x_1y_1$$
$$+ x_2y_2$$
$$+ x_3y_3$$

In [87]:

```
x.dot(y) # dot product 1*4 + 2*5 + 3*6
```

Out[87]:

```
32
```

In [88]:

```
z = np.array([y, y**2])
print(len(z)) # number of rows of array
```

```
2
```

Let's look at transposing arrays. Transposing permutes the dimensions of the array.

In [81]:

```
z = np.array([y, y**2])
```

```
z
```

```
Out[81]:
```

```
array([[ 4,  5,  6],  
       [16, 25, 36]])
```

The shape of array `z` is `(2, 3)` before transposing.

```
In [82]:
```

```
z.shape
```

```
Out[82]:
```

```
(2, 3)
```

Use `.T` to get the transpose.

```
In [83]:
```

```
z.T
```

```
Out[83]:
```

```
array([[ 4, 16],  
       [ 5, 25],  
       [ 6, 36]])
```

The number of rows has swapped with the number of columns.

```
In [84]:
```

```
z.T.shape
```

```
Out[84]:
```

```
(3, 2)
```

Use `.dtype` to see the data type of the elements in the array.

```
In [85]:
```

```
z.dtype
```

```
Out[85]:
```

```
dtype('int32')
```

Use `.astype` to cast to a specific type.

```
In [87]:
```

```
z = z.astype('f')  
z.dtype
```

```
Out[87]:
```

```
dtype('float32')
```



**Numpy has many built in math functions that can be performed on arrays.**

In [88]:

```
a = np.array([-4, -2, 1, 3, 5])
```

In [89]:

```
a.sum()
```

Out[89]:

3

In [90]:

```
a.max()
```

Out[90]:

5

In [91]:

```
a.min()
```

Out[91]:

-4

In [92]:

```
a.mean()
```

Out[92]:

0.6

In [93]:

```
a.std()
```

Out[93]:

3.2619012860600183

`argmax` and `argmin` return the index of the maximum and minimum values in the array.

In [94]:

```
a.argmax()
```

Out[94]:

4

In [95]:

```
a.argmin()
```

Out[95]:

0

In [98]:

```
a.cumsum()
```

Out[98]:

```
array([-4, -6, -5, -2,  3], dtype=int32)
```

## Indexing / Slicing

In [99]:

```
s = np.arange(13)**2
s
```

Out[99]:

```
array([ 0,  1,  4,  9, 16, 25, 36, 49, 64, 81, 100, 121, 144],
      dtype=int32)
```

**Use bracket notation to get the value at a specific index. Remember that indexing starts at 0.**

In [100]:

```
s[0], s[4], s[-1]
```

Out[100]:

```
(0, 16, 144)
```

**Use `:` to indicate a range.** `array[start:stop]`

**Leaving `start` or `stop` empty will default to the beginning/end of the array.**

In [101]:

```
s[1:5]
```

Out[101]:

```
array([ 1,  4,  9, 16], dtype=int32)
```

**Use negatives to count from the back.**

In [102]:

```
s[-4:]
```

Out[102]:

```
array([ 81, 100, 121, 144], dtype=int32)
```

**A second `:` can be used to indicate step-size.** `array[start:stop:stepsize]`

**Here we are starting 5th element from the end, and counting backwards by 2 until the beginning of the array is reached.**

In [103]:

```
s[-5::-2]
```

Out[103]:

```
array([64, 36, 16,  4,  0], dtype=int32)
```

**Let's look at a multidimensional array.**

In [107]:

```
r = np.arange(36)
r.resize((6, 6))
r
```

Out[107]:

```
array([[ 0,  1,  2,  3,  4,  5],
       [ 6,  7,  8,  9, 10, 11],
       [12, 13, 14, 15, 16, 17],
       [18, 19, 20, 21, 22, 23],
       [24, 25, 26, 27, 28, 29],
       [30, 31, 32, 33, 34, 35]])
```

In [108]:

```
r.resize((3,4,3))
print(r)
```

```
[[[ 0  1  2]
   [ 3  4  5]
   [ 6  7  8]
   [ 9 10 11]]

 [[12 13 14]
  [15 16 17]
  [18 19 20]
  [21 22 23]]

 [[24 25 26]
  [27 28 29]
  [30 31 32]
  [33 34 35]]]
```

In [105]:

```
r[2, 2]
```

Out[105]:

14

**And use : to select a range of rows or columns**

In [106]:

```
r[3, 3:6]
```

Out[106]:

```
array([21, 22, 23])
```

**Here we are selecting all the rows up to (and not including) row 2, and all the columns up to (and not including) the last column.**

In [112]:

```
r[:2, :-1]
```

Out[112]:

```
array([[ 0,  1,  2,  3,  4],
       [ 6,  7,  8,  9, 10]])
```

**This is a slice of the last row, and only every other element.**

In [113]:

```
r[-1, ::2]
```

Out[113]:

```
array([30, 32, 34])
```

**We can also perform conditional indexing. Here we are selecting values from the array that are greater than 30. (Also see `np.where`)**

In [114]:

```
r[r > 30]
```

Out[114]:

```
array([31, 32, 33, 34, 35])
```

**Here we are assigning all values in the array that are greater than 30 to the value of 30.**

In [115]:

```
r[r > 30] = 30  
r
```

Out[115]:

```
array([[ 0,  1,  2,  3,  4,  5],  
       [ 6,  7,  8,  9, 10, 11],  
       [12, 13, 14, 15, 16, 17],  
       [18, 19, 20, 21, 22, 23],  
       [24, 25, 26, 27, 28, 29],  
       [30, 30, 30, 30, 30, 30]])
```

## Copying Data

**Be careful with copying and modifying arrays in NumPy!**

`r2` is a slice of `r`

In [116]:

```
r2 = r[:3, :3]  
r2
```

Out[116]:

```
array([[ 0,  1,  2],  
       [ 6,  7,  8],  
       [12, 13, 14]])
```

**Set this slice's values to zero (`[:]` selects the entire array)**

In [117]:

```
r2[:] = 0  
r2
```

Out[117]:

```
array([[0, 0, 0],  
       [0, 0, 0],  
       [0, 0, 0]])
```

```
[0, 0, 0]])
```

**Use bracket notation to slice:** `array[row, column]`

`r` has also been changed!

In [118]:

```
r
```

Out[118]:

```
array([[ 0,  0,  0,  3,  4,  5],
       [ 0,  0,  0,  9, 10, 11],
       [ 0,  0,  0, 15, 16, 17],
       [18, 19, 20, 21, 22, 23],
       [24, 25, 26, 27, 28, 29],
       [30, 30, 30, 30, 30, 30]])
```

**To avoid this, use `r.copy` to create a copy that will not affect the original array**

In [119]:

```
r_copy = r.copy()
r_copy
```

Out[119]:

```
array([[ 0,  0,  0,  3,  4,  5],
       [ 0,  0,  0,  9, 10, 11],
       [ 0,  0,  0, 15, 16, 17],
       [18, 19, 20, 21, 22, 23],
       [24, 25, 26, 27, 28, 29],
       [30, 30, 30, 30, 30, 30]])
```

**Now when `r_copy` is modified, `r` will not be changed.**

In [120]:

```
r_copy[:] = 10
print(r_copy, '\n')
print(r)
```

```
[[10 10 10 10 10 10]
 [10 10 10 10 10 10]
 [10 10 10 10 10 10]
 [10 10 10 10 10 10]
 [10 10 10 10 10 10]
 [10 10 10 10 10 10]]
```

```
[[ 0  0  0  3  4  5]
 [ 0  0  0  9 10 11]
 [ 0  0  0 15 16 17]
 [18 19 20 21 22 23]
 [24 25 26 27 28 29]
 [30 30 30 30 30 30]]
```

## Iterating Over Arrays

Let's create a new 4 by 3 array of random numbers 0-9.

In [121]:

```
test = np.random.randint(0, 10, (4,3))
test
```

Out[121]:

```
array([[1, 0, 5],
       [8, 7, 0],
       [8, 0, 6],
       [6, 6, 7]])
```

### Iterate by row:

In [122]:

```
for row in test:
    print(row)
```

```
[1 0 5]
[8 7 0]
[8 0 6]
[6 6 7]
```

### Iterate by index:

In [123]:

```
for i in range(len(test)):
    print(test[i])
```

```
[1 0 5]
[8 7 0]
[8 0 6]
[6 6 7]
```

### Iterate by row and index:

In [124]:

```
for i, row in enumerate(test):
    print('row', i, 'is', row)
```

```
row 0 is [1 0 5]
row 1 is [8 7 0]
row 2 is [8 0 6]
row 3 is [6 6 7]
```

### Use `zip` to iterate over multiple iterables.

In [125]:

```
test2 = test**2
test2
```

Out[125]:

```
array([[ 1,  0, 25],
       [64, 49,  0],
       [64,  0, 36],
       [36, 36, 49]], dtype=int32)
```

In [126]:

```
for i, j in zip(test, test2):
```

```
print(i, '+', j, '=', i+j)
```

```
[1 0 5] + [ 1 0 25] = [ 2 0 30]  
[8 7 0] + [64 49 0] = [72 56 0]  
[8 0 6] + [64 0 36] = [72 0 42]  
[6 6 7] + [36 36 49] = [42 42 56]
```

In [ ]: